

**Aval, Labbé, q-analogs of rational numbers:
from Ostrowski numeration systems
to perfect matchings, arXiv:2511.11290**

$\frac{29}{12}$ $\xrightarrow{\text{CF}_{\text{even}}}$ $[2, 2, 2, 2]$ \xrightarrow{W} 1100110 $\xrightarrow{\theta}$ 0110011

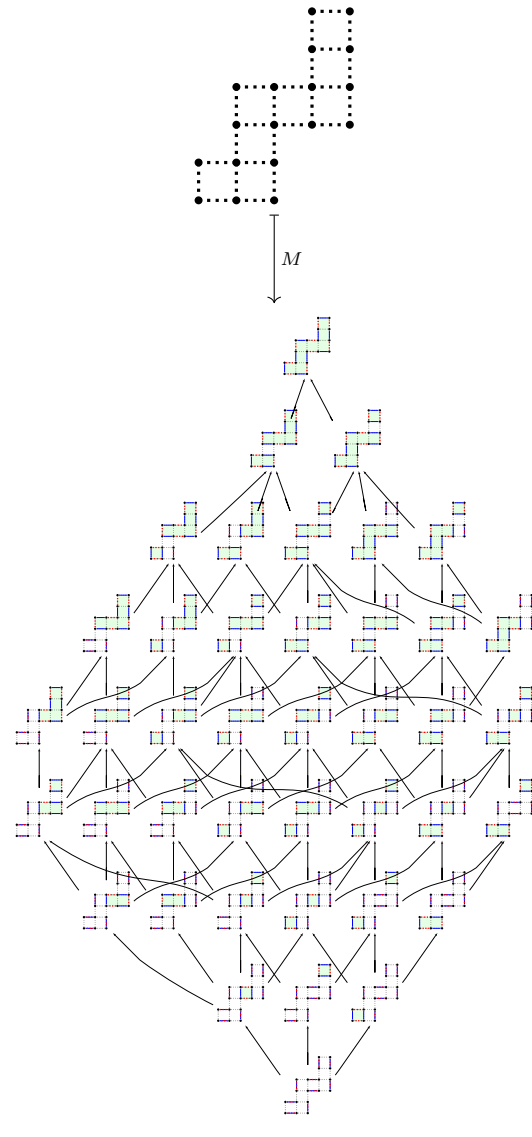
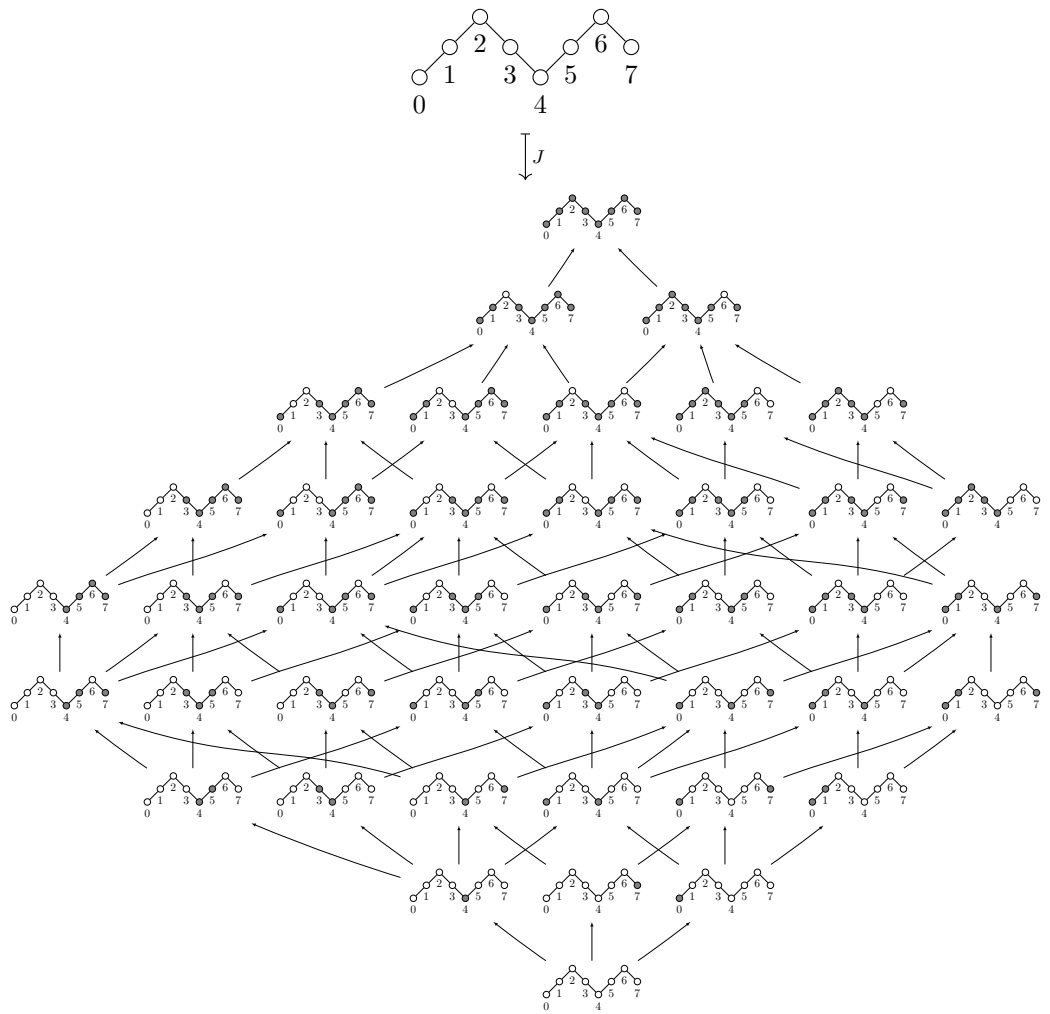
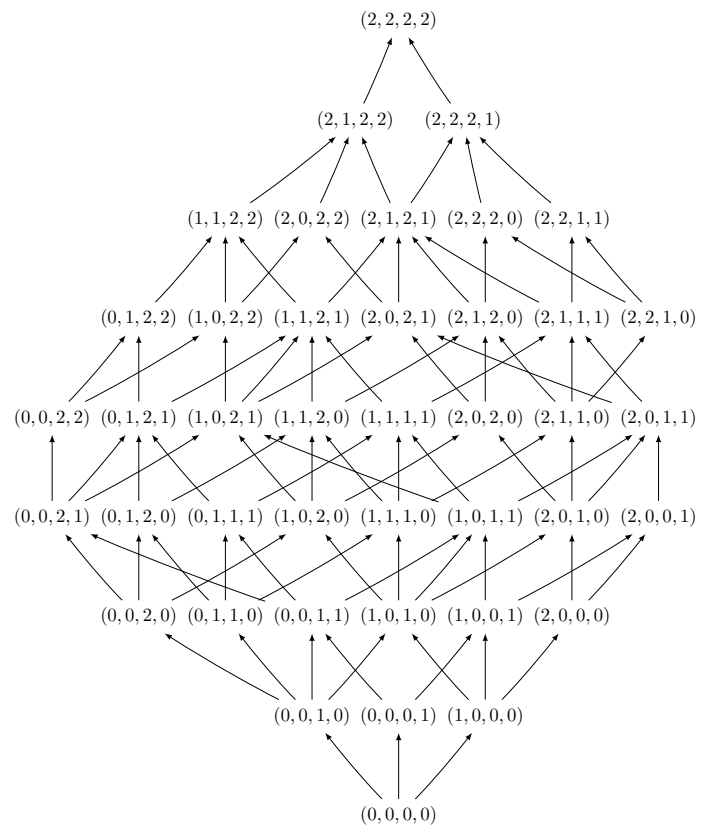
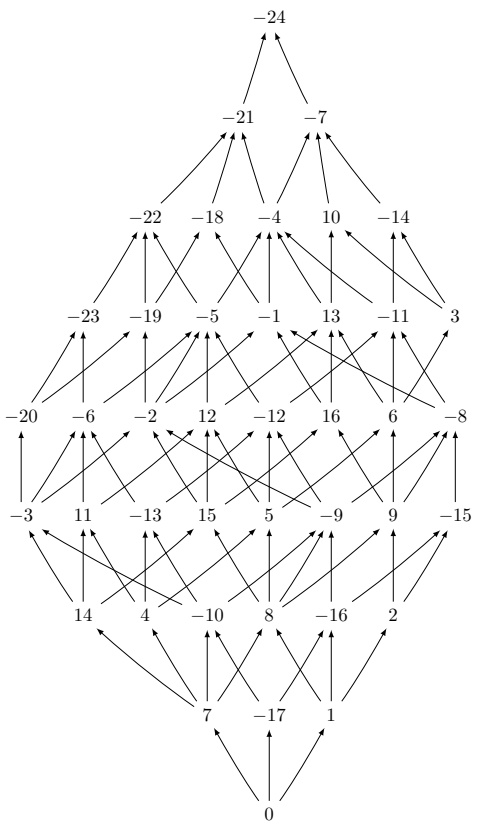
\mathcal{B}

F

G

J

M



$\mathcal{Z}([2, 2, 2, 2]) = \mathbb{Z} \cap [-24, 17]$

$\mathcal{B}([2, 2, 2, 2]) \xleftarrow{\text{val}}$

Ψ

$\mathcal{J}(\frac{29}{12})$

Φ

$\mathcal{M}(\frac{29}{12})$

$(r_0, -r_1, r_2, -r_3) = (1, -3, 7, -17)$
 $r_4 = 41$

$\left[\frac{29}{12} \right]_q = q^{-1} \frac{q^8 + 2q^7 + 5q^6 + 6q^5 + 6q^4 + 5q^3 + 3q^2 + q}{q^5 + 2q^4 + 3q^3 + 3q^2 + 2q + 1}$